

npda : $M = (Q, \Sigma, \Gamma, \delta, q_0, z, F)$

$\delta: (q_i, a, b) = (q_j, x) \quad x \in \Gamma^*$

create a npda (pda) for L :

$L_1 = \{a^n b^{n+1} : n \geq 0\} = \{b, abb, aabbb, \dots\}$

algorithm : • push extra 'a' first

• push 'a' from input stream

• match 'b' w/ 'a' - pop 'a'.

• input stream empty (done) + stack
start symbol on top of stack
go to final.

$M = (\dots)$

$L_2 = \{a^{2n} b^n : n \geq 1\}$

$L_3 = \{a^n b^{n+1} : n \geq 1\}$

$L_4 = \{w : n_a(w) = 2n_b(w) : w \in \{a, b\}^*\}$